

Application of acoustic method for determination of coordinates of leakage in cavities bounded by large surfaces

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Introduction

An acoustic correlation measuring method is successfully applied for determination of co-ordinates of leakage in the pipelines transporting gas products [1]. When performing mathematical calculations the spatial dimensions of the pipelines are not estimated [2,3]. In that case it is assumed that the pipeline is a one-dimensional formation. But very often the leakproofness of various reservoirs, vessels and other hollow spaces bounded by large dimension surfaces are investigated. When exploring such objects two-dimensional coordinates are needed for determination of the place of leakage. In that case, to determine the location of leakage points on the surface of cavities the two- dimensional problem has to be solved.

Theoretical analysis

Let us assume that there is a conventional cavity wall surface. The gas gushing at the leakage points of that surface generates acoustical noises. These noises propagating on the surface of that plane reach the points F_0 and F_1 . At these points electroacoustical transducers register acoustical noises. If the speed of sound in the wall of cavity is c , and the time of propagation of acoustic noises from the leakage place S to the focus point F_0 is t_0 , then the distance r_0 from the leakage place S to the focus point F_0 may be determined by equation $r_0=ct_0$. By analogy, the distance $r_1=ct_1$, where t_1 is the time of propagation of noises from S to the focus point F_1 . The difference Δt_1 of times of propagation of acoustical noises from the leakage point S to the electroacoustical transducers F_0 and F_1 may be determined as

$$\Delta t_1 = t_0 - t_1 = \frac{r_0 - r_1}{c}. \quad (1)$$

After applying the theorem of cosines it may be written

$$r_1^2 = r_0^2 + d_1^2 - 2r_0d_1 \cos(\gamma_1). \quad (2)$$

Here d_1 is the distance between electroacoustical transducers, γ_1 is the angle between d_1 and r_0 . Solving the system of Eq. 1 and 2 enables to eliminate r_1 and to determine r_0 :

$$r_0 = \frac{c^2 (\Delta t_1)^2 - d_1^2}{2[c\Delta t_1 - d_1 \cos(\gamma_1)]}. \quad (3)$$

How one can see from Eq 3 all terms on the right side, except the angle γ_1 , are measurable or selectable parameters. Thus, the distance r_0 is the function of angle γ_1 : $r_0=r_0(\gamma_1)$.

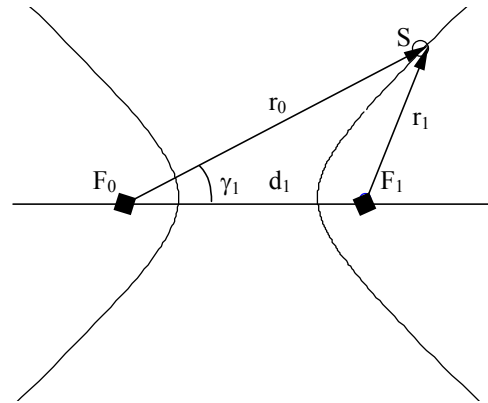


Fig.1. Determination of leakage coordinates on the plane by using one pair of electroacoustical transducers

Since the difference of distances of propagation of acoustical noises from the leakage place S to the electroacoustical transducers F_0 and F_1 $\Delta r = r_0 - r_1$ is constant, the radius vector will draw a hyperbola on the plane when the angle γ is changed (Fig.1). It means that any point of hyperbola may be the point of leakage. With the purpose to avoid ambiguity, we supplement the measuring system with one more electroacoustical transducer located at the point F_2 (Fig.2). When analysing the propagation of acoustical noises from the leakage place S to electroacoustical transducers F_0 and F_2 , it will be obtained that

$$r_0 = \frac{c^2 (\Delta t_2)^2 - d_2^2}{2[c\Delta t_2 - d_2 \cos(\gamma_2)]}. \quad (4)$$

It can be seen from Fig.2 that $\gamma_2 = \gamma_1 - \alpha$, where α is an angle between the straight lines F_0F_1 and F_0F_2 . When

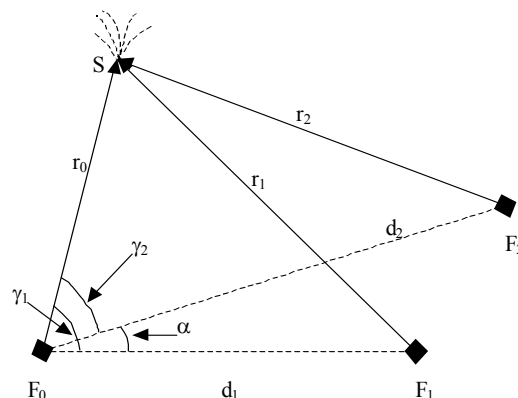


Fig.2. Determination of leakage co-ordinates by using two pairs of electroacoustical transducers

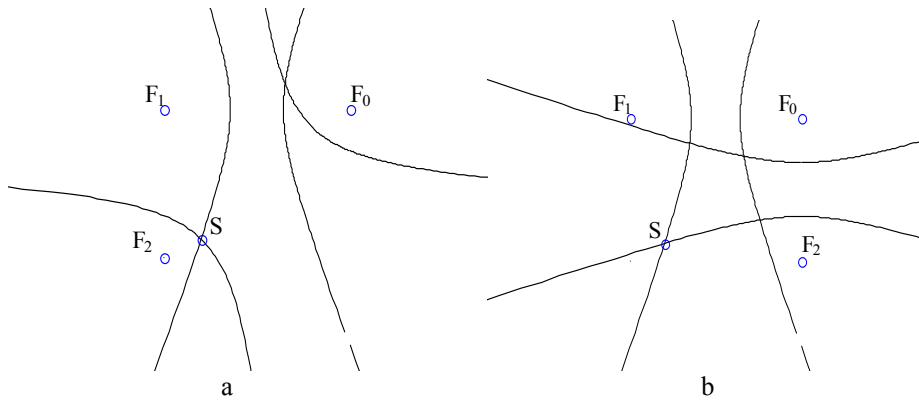


Fig.3. Probable points of leakage: a - 2, b - 4

equalizing Eq. 3 and 4 and replacing the angle γ_2 with the expression $\gamma_2 = \gamma_1 - \alpha$, one can obtain

$$\frac{c^2 \Delta t_1^2 - d_1^2}{c \Delta t_1 - d_1 \cos(\gamma_1)} = \frac{c^2 \Delta t_2^2 - d_2^2}{c \Delta t_2 - d_2 \cos(\gamma_1 - \alpha)}. \quad (5)$$

After the transformation of this equation

$$(c^2 \Delta t_1^2 - d_1^2)[c \Delta t_2 - d_2 \cos(\gamma_1) \cos(\alpha) - d_2 \sin(\gamma_1) \sin(\alpha)] = (c^2 \Delta t_2^2 - d_2^2)[c \Delta t_1 - d_1 \cos(\gamma_1)] \quad (6)$$

and introducing the notations

$$\begin{aligned} A &= (c^2 \Delta t_1^2 - d_1^2) c \Delta t_2, \\ B &= (c^2 \Delta t_1^2 - d_1^2) d_2 \cos(\alpha), \\ C &= (c^2 \Delta t_1^2 - d_1^2) d_2 \sin(\alpha), \\ D &= (c^2 \Delta t_2^2 - d_2^2) c \Delta t_1, \\ E &= (c^2 \Delta t_2^2 - d_2^2) d_1, \end{aligned} \quad (7)$$

it can be obtained:

$$A - B \cos(\gamma_1) - C \sin(\gamma_1) = D - E \cos(\gamma_1). \quad (8)$$

In Eq. 8 we express $\sin(\gamma_1)$ by $\cos(\gamma_1)$ and introduce notations:

$$\begin{aligned} M &= (B - E)^2 + C^2 \\ N &= (A - D)(B - E) \\ L &= (A - D)^2 - C^2 \end{aligned} \quad (9)$$

After some algebraic operations one can obtain a quadratic equation:

$$M \cos^2(\gamma_1) - 2N \cos(\gamma_1) + L = 0. \quad (10)$$

Solving this equation one can find out an expression for the angle γ_1

$$\gamma_1 = \arccos \left(\frac{N \pm \sqrt{N^2 - ML}}{M} \right). \quad (11)$$

For simplification of calculations when using Eq. 11 one can return to the notations applied in Eq. 7:

$$\gamma_1 = \arccos \left\{ \frac{(A - D)(B - E) \pm \sqrt{(B - E)^2 - (A - D)^2 + C^2}}{\sqrt{(B - E)^2 + C^2}} \right\} \quad (12)$$

After analysing Eq. 12 it can be seen that in the interval $0 \leq \gamma_1 < 2\pi$ depending on the coordinates of the

leakage and the location of electroacoustical transducers the Eq. 12 may have 2, 3 or 4 real solutions (Fig.3).

With the purpose to determine which of the determined values of the angle γ_1 between d_1 and r_0 is true, let us introduce one more electroacoustical transducer F_3 . By analogy to the case described earlier, when coupling the new transducer F_3 with the transducer F_0 , one can obtain

$$r_0 = \frac{c^2 (\Delta t_3)^2 - d_3^2}{2[c \Delta t_3 - d_3 \cos(\gamma_1 - \beta)]}. \quad (13)$$

Here β is the angle between the straight lines connecting the pairs of transducers $F_0 F_1$ and $F_0 F_3$. Substituting the value γ_1 in Eq. 13 with the solution, obtained by solving Eq. 12, the values of r_0 can be calculated. After that we compare the results of calculation obtained by using the algorithms 3 and 13 when the values of angle γ_1 are the same. The value of r_0 , which is the same when applying Eq. 3 and 13, is considered to be the true distance from the electroacoustical transducer F_0 . The value of angle γ_1 , which corresponds to this distance, is the true value of angle between d_1 and r_0 (Fig.4).

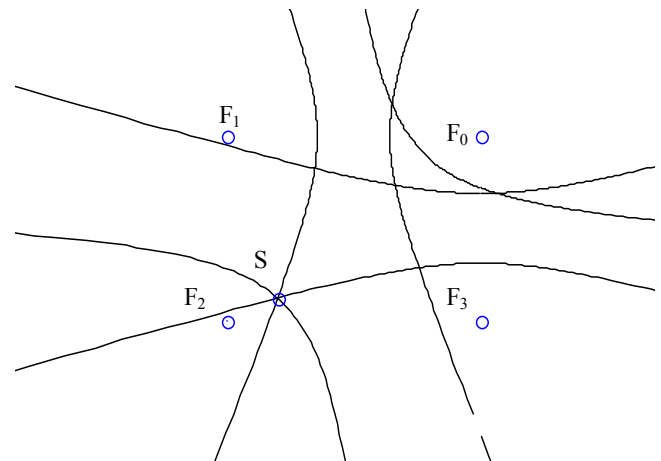


Fig.4. Unambiguous determination of leakage coordinates by using three pairs of independent electroacoustical transducers

Analysis of the results of calculation shows that when using three independent pairs of electroacoustical transducers and applying algorithm (3) three hyperbolas are obtained and they have only one common point of

intersection. This point corresponds to the leakage place on the plane of measurements. In this way it is possible to determine the position of leakage on the plane unambiguously when the values of the angle γ_1 and the distance r_0 are known.

Conclusion

The great actuality of assurance of the leakproofness of reservoirs, vessels and other cavities bounded by the large dimension surfaces was shown.

Noval method and algorithms were proposed for determination of coordinates of the noise source in the two-dimensional area.

The proposed method and algorithms might be used while developing ultrasonic systems for detection of leakage and determination of its coordinates when the cavities (hollows) are bounded by large plane surfaces.

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Akustinio metodo taikymas dideliais paviršiais apribotų ertmių nesandarumų koordinatėms nustatyti

Reziومه

Nustatant dideliais paviršiais apribotų talpyklų nesandarių vietų koordinatas, būtina spręsti dvimatį uždavinį. Tokiu atveju, koreliaciniu metodu nustatant galimo nehermetiškumo koordinatas plokštumoje pagal akustinių triukšmų sklaidimo nuo nuotėkio vietos iki elektroakustinių keitiklių laikų skirtumą, rezultatas gaunamas daugiareikšmis. Galimos nesandarios vietos atitinka hiperboles, kurių židiniuose išdėstyti elektroakustiniai keitikliai. Naudojant trečią elektroakustinį keitiklį, nesandari vieta plokštumoje gali būti aprašoma lygčių sistema, kuri priklausomai nuo hermetiškumo pažeidimo vietos ir elektroakustinių keitiklių tarpusavio padėties gali turėti 2, 3 arba 4 realius sprendinius. Parodoma, kad, siekiant vienareikšmiško sprendinio, būtinas dar vienas elektroakustinis keitiklis. Pasiūlyta metodika ir algoritmai gali būti taikomi kuriant ultragarsines sistemas didelių talpyklų ir rezervuarų nesandarumams aptikti ir jų koordinatėms nustatyti.

Pateikta spaudai: 2001 03 12

DOI: 10.5755/j01.u.38.1.8045